

## CTEQ task force on $W$ and $Z$ boson physics

J. Huston, Pavel Nadolsky (convener), J. Pumplin, D. Stump,  
W.-K. Tung, C.-P. Yuan, ...

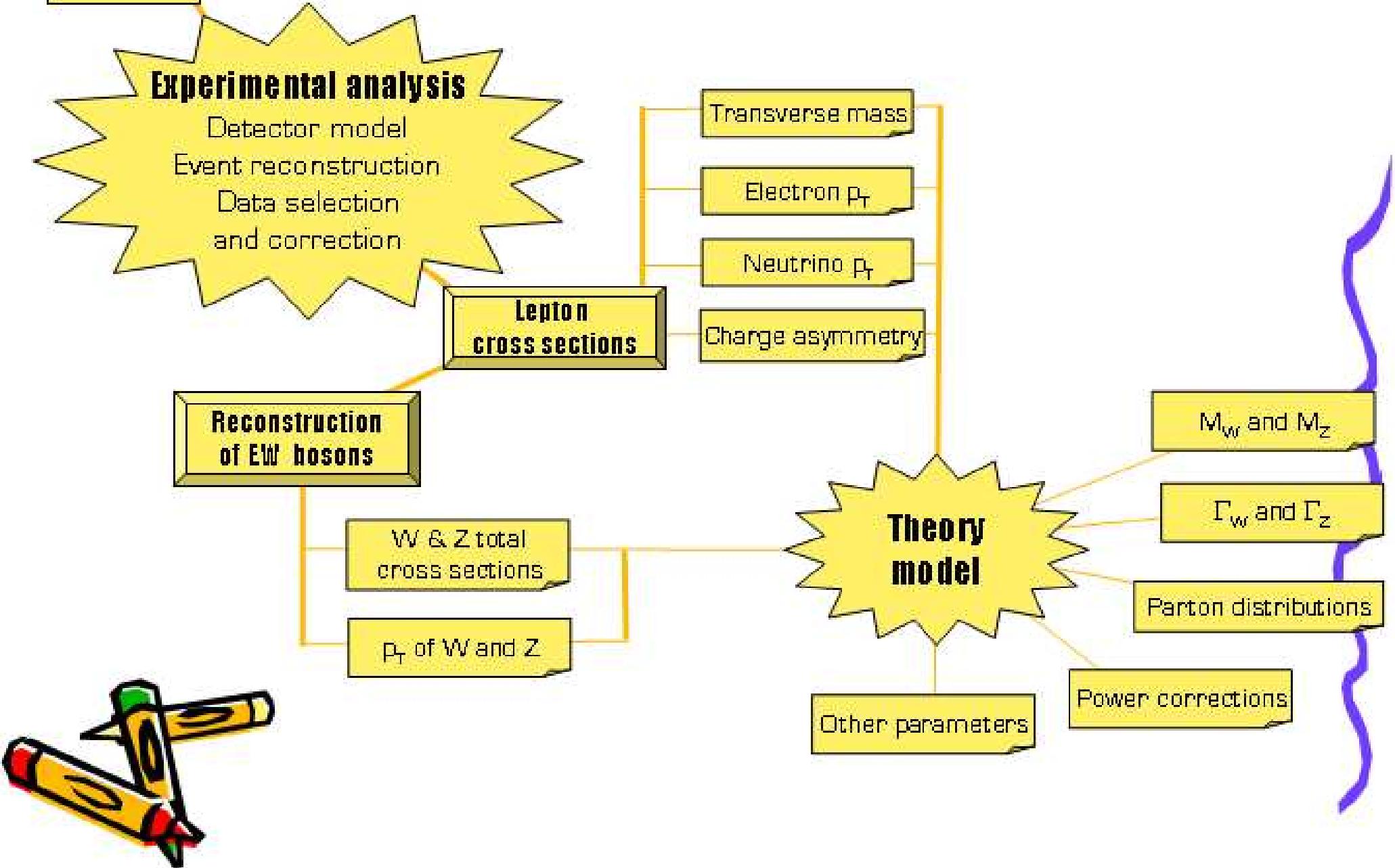
Objective:

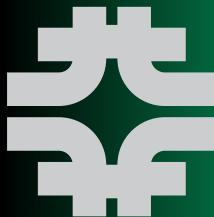
- ✓ high-precision model for  $W$  and  $Z$  boson observables
- ✓ predict uncertainties for the Run-2 measurement of
  - ◆  $W$  and  $Z$  total cross sections,
  - ◆  $M_W$ ,
  - ◆  $p_T$  distributions,
  - ◆ ...

Collaboration with experimental groups

☞ decide on contact persons from CDF and DØ

# W & Z boson production at the Tevatron





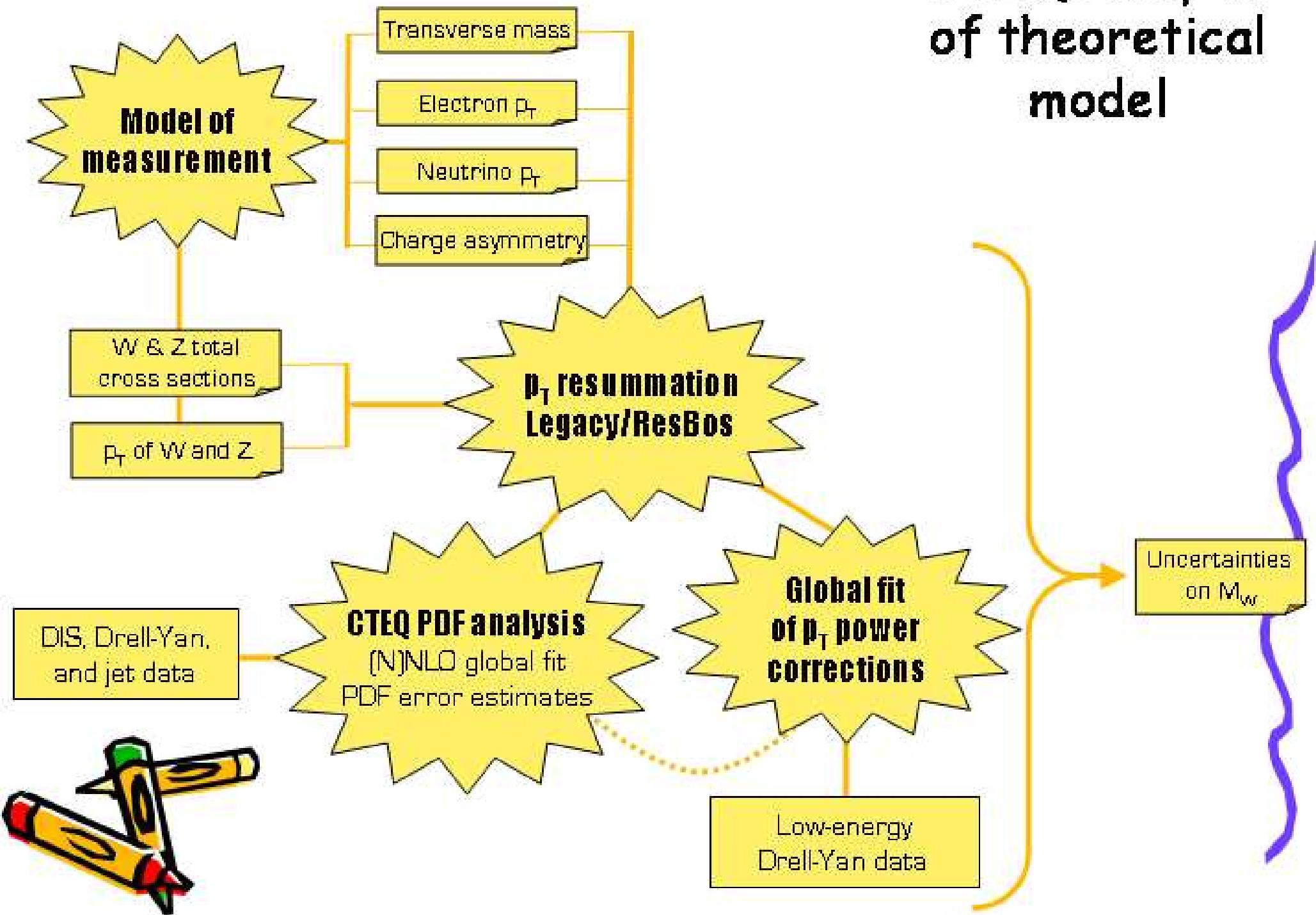
## Variations in the fitted $M_W$ in Run-1 (in MeV)

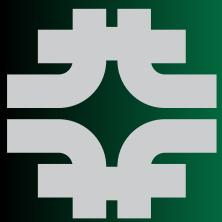
|                   | Central electrons<br>( $ y_\ell  \leq 1$ ) |                             |                               | Forward electrons<br>( $1 \leq  y_\ell  \leq 2.5$ ) |                             |                               |
|-------------------|--|-----------------------------|-------------------------------|---|-----------------------------|-------------------------------|
| Source            | $\delta M_W$<br>( $m_T$ )                  | $\delta M_W$<br>( $p_T^e$ ) | $\delta M_W$<br>( $p_T^\nu$ ) | $\delta M_W$<br>( $m_T$ )                           | $\delta M_W$<br>( $p_T^e$ ) | $\delta M_W$<br>( $p_T^\nu$ ) |
| statistics        | 70   | 85                          | 105                           | 107   | 128                         | 159                           |
| $p_T(W)$ spectrum | 10   | 50                          | 25                            | 22  | 37                          | 44                            |
| MRSR2             | 5  | 26                          | 3                             | -11   | -21                         | -43                           |
| MRS(A')           | -5   | 16                          | -31                           | -7  | -43                         | -19                           |
| CTEQ5M            | -8   | 6                           | -22                           | 14  | 9                           | -17                           |
| CTEQ4M            | 10   | 11                          | -18                           | 1   | -21                         | 22                            |
| CTEQ3M            | 0  | 64                          | -9                            | 13  | 30                          | 28                            |
| (Many) other      | ...  | ...                         | ...                           | ...   | ...                         | ...                           |

*DØ Collaboration, Phys. Rev. D62, 092006 (2000)*

Many sources of sizeable correlated errors

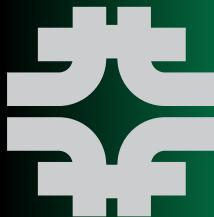
# CTEQ analysis of theoretical model





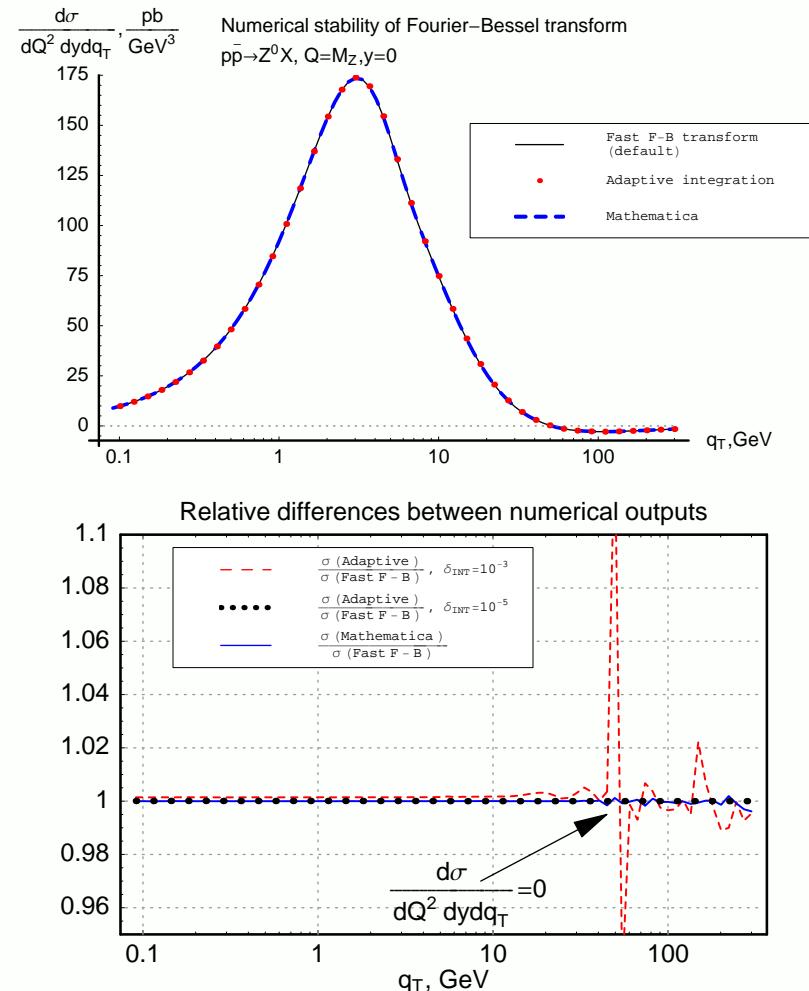
## Simplified model of experimental measurements

- ✓ Central ( $-1 \leq y_e \leq 1$ ) and forward ( $|y_e| > 1$ ) regions
- ✓  $p_{T e} > 25$  GeV
- ✓ Missing  $p_T > 25$  GeV
- ✓ Electron energy smearing
- ✓ ...?

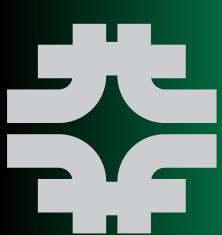


## Fast and accurate resummation program

- ✓ Resummation part re-written in C++
- ✓ Adaptive integration and fast Fourier-Bessel transform routines
- ✓ Improvement up to a factor 800 (80000%) in speed
- ✓ Accuracy of F-B transform better than 0.1% at  $q_T^2 \ll M_W^2$



Suitable for intensive CPU calculations within the CTEQ fitting analysis



## Universality of resummed $q_T$ distributions in $h_1 h_2 \rightarrow V X$

(Landry, Brock, P.N., Yuan, Phys.Rev. D67, 073016 (2003))

As PDF's include the universal nonperturbative part, resummed  $q_T$  distributions are expected to include a universal nonperturbative function

$$\frac{d\sigma}{dx_1 dx_2 dq_T^2} \Big|_{q_T \rightarrow 0} \propto \int \frac{d^2 b}{(2\pi)^2} e^{i\vec{q}_T \cdot \vec{b}} W^{\text{pert}}(b, x_1, x_2) e^{-S^{NP}(b, Q, x_1, x_2)},$$

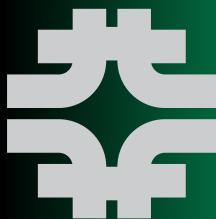
where

$$S^{NP}(b) = b^2 (g_1 + g_2 \ln Q) \quad (\text{Davies, Webber, Stirling, 1985})$$

$$S^{NP}(b) = b^2 (g_1 + g_2 \ln Q) + b g_1 g_3 \ln (100 x_1 x_2) \quad (\text{Ladinsky, Yuan, 1993})$$

$$S^{NP}(b) = b^2 (g_1 + g_2 \ln Q + g_1 g_3 \ln (100 x_1 x_2)) \quad (\text{BLNY, 2002})$$

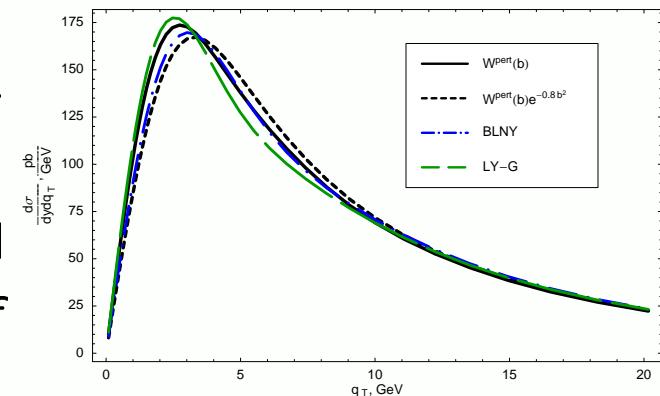
The last form more preferable theoretically (CSS; Korchemsky, Sterman)



## Are nonperturbative contributions important for Tevatron?

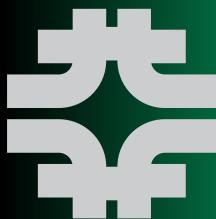
We find strong sensitivity of the Run 1  $Z$  data to  $S^{NP}(b)$  at  $q_T \lesssim 10$  GeV

Recently, Qiu and Zhang suggested that such dependence may be an artifact of “ $b_*$  prescription” for  $S^{NP}(b)$ . They suggest that  $Z$  data is described well just by the perturbative part of the resummed cross section



While  $W$  and  $Z$  boson cross sections are dominated by perturbative terms, neglecting (or changing)  $S^{NP}(b)$  may shift the peak of  $d\sigma/dq_T$  by 200-500 MeV (large effect given a targeted  $\delta M_W \sim 50$  MeV)

- ✿ The global analysis of  $S^{NP}(b, Q)$  and its  $Q$  dependence remains very necessary



## Nonperturbative function in the resummation formalism

BLNY study:

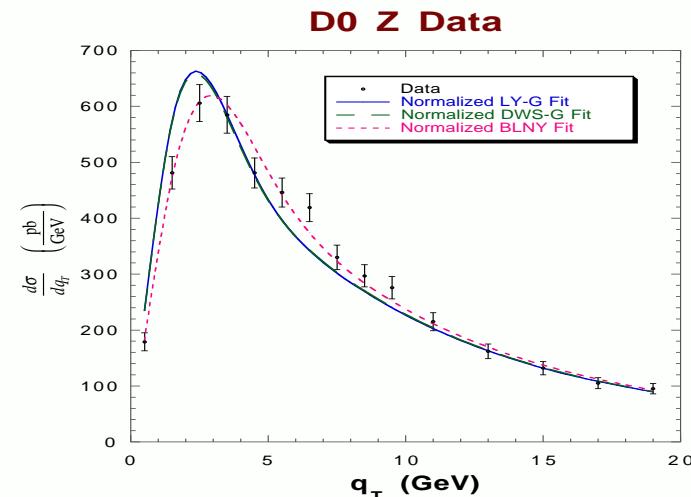
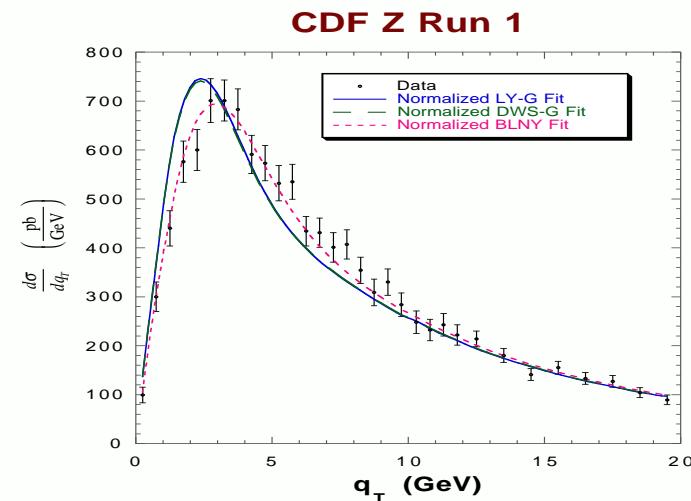
- ✓ first global fit of the Drell-Yan and Tevatron Run 1  $Z$  data

- ✓ extended set of data ( $\sim 100$  data points vs. 31 point in earlier studies)

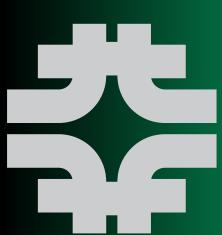
- ✓ All 3 forms of  $S^{NP}(b)$  updated

- ✓ Gaussian form (BLNY) strongly preferred by the data;

$\chi^2/d.o.f. = 176/119 \sim 1.48$  vs. 3.42 and 3.47 for other forms

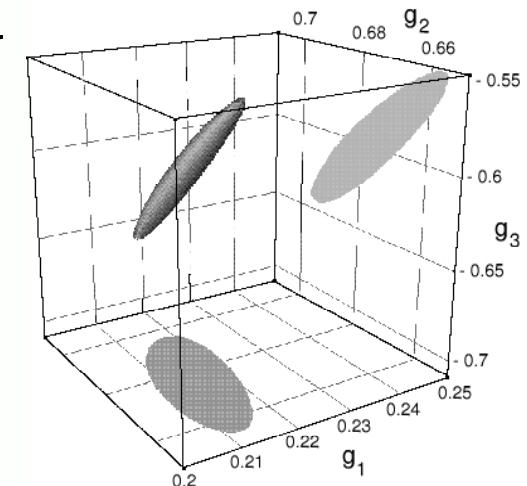


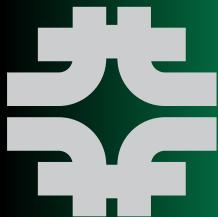
❖ Strong evidence for universality of  $S^{NP}(b, Q)$



## Nonperturbative contributions: further studies

- ✓ Explore new proposals for the model of nonperturbative terms
- ✓ Examine an updated  $b_*$  prescription with  $b_{max} \sim 1 \text{ GeV}^{-1}$
- ✓ Obtain true confidence intervals for  $S^{NP}(b, Q)$  in presence of systematical errors
- ✓ Study correlation between nonperturbative Sudakov factor  $S^{NP}(b, Q)$  and parton distributions
  - ◆ Refit  $S^{NP}(b, Q)$  for 41 eigenvector PDF sets
  - ◆ Merge global fits of the PDFs and  $p_T$  distributions

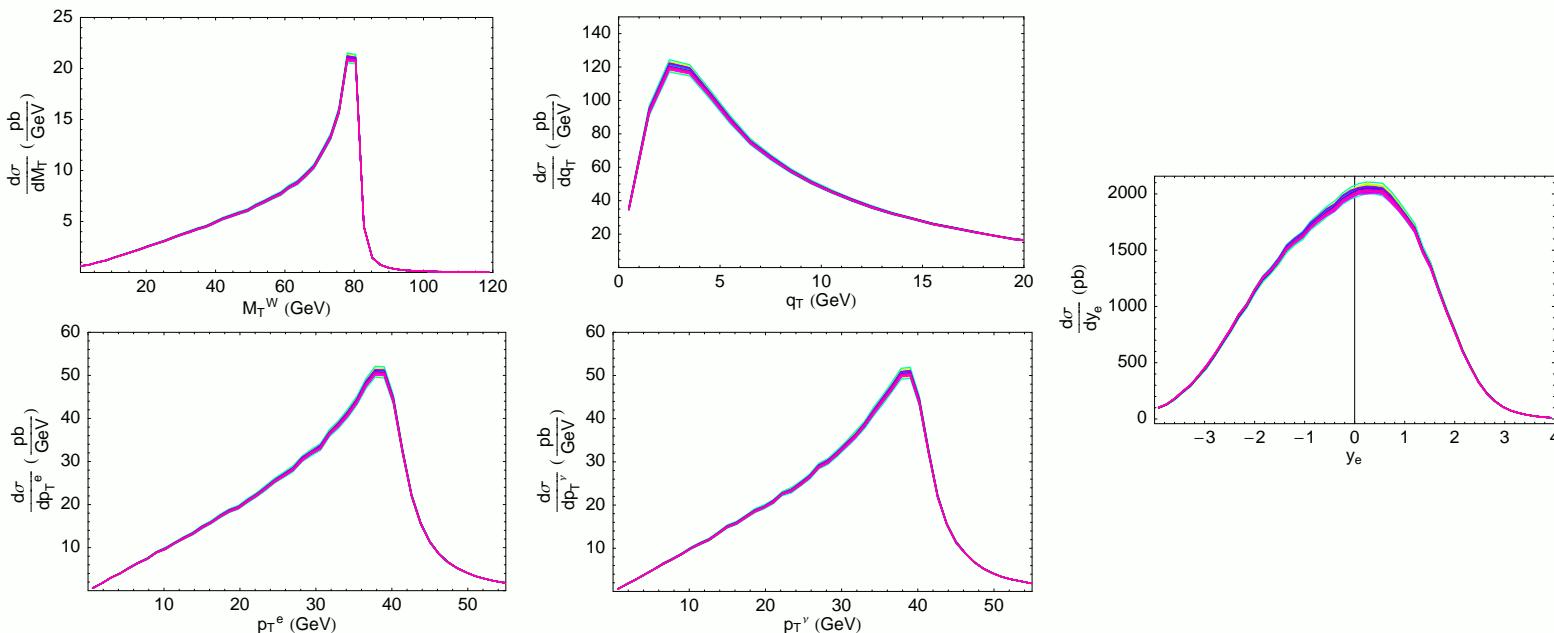




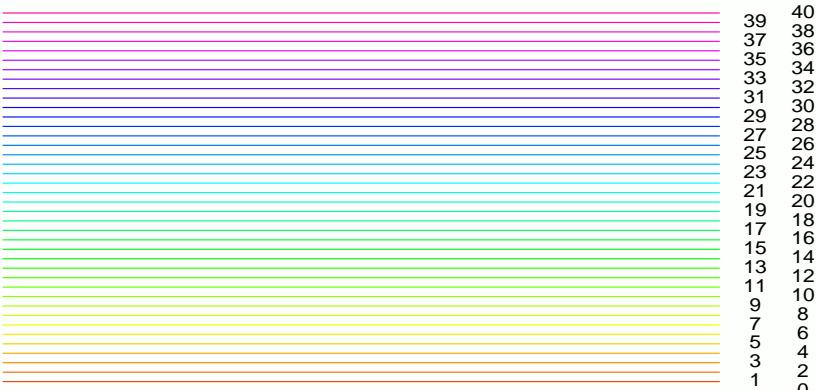
## Global analysis (CTEQ)

- ✓ Analysis of a large data set ( $\sim 2000$  data points) from deep inelastic scattering, lepton pair and jet production
- ✓ Methods for handling many ( $\sim 200$ ) sources of systematic errors
- ✓ Complete analysis of the PDF parameter space in the vicinity of  $\min \chi^2$  with inclusion of all published correlated systematic errors
- ✓ Quantitative estimates of uncertainties in the PDFs and physical observables
  - ◆ Lagrange mutliplier method
  - ◆ 1 central PDF set +  $20 \times 2$  extreme PDF sets 
    - \* Calculate the observable 41 times
    - \* Calculate PDF uncertainty using a master formula

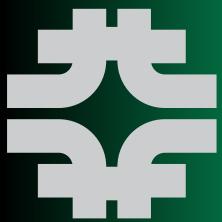
# $W^+$ production at $\sqrt{s} = 1.96$ TeV; $M_W = 80.423$ GeV; no lepton cuts



Color legend for PDF sets



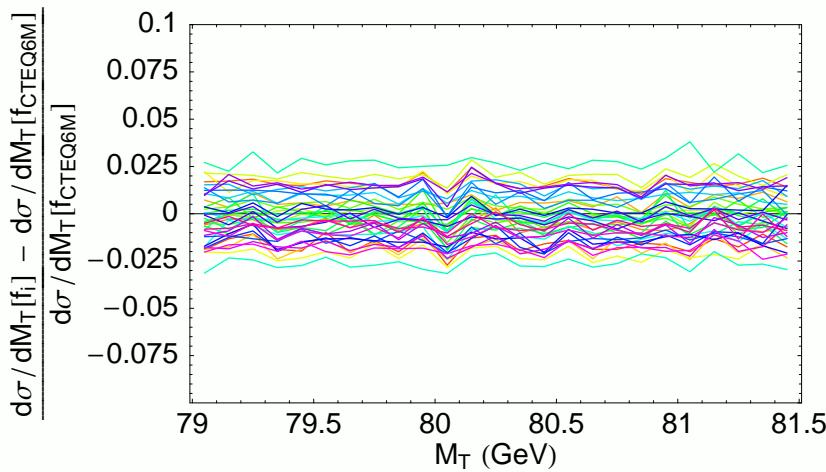
Concentrate on the ratios to  
the distribution for CTEQ6M  
PDF set instead



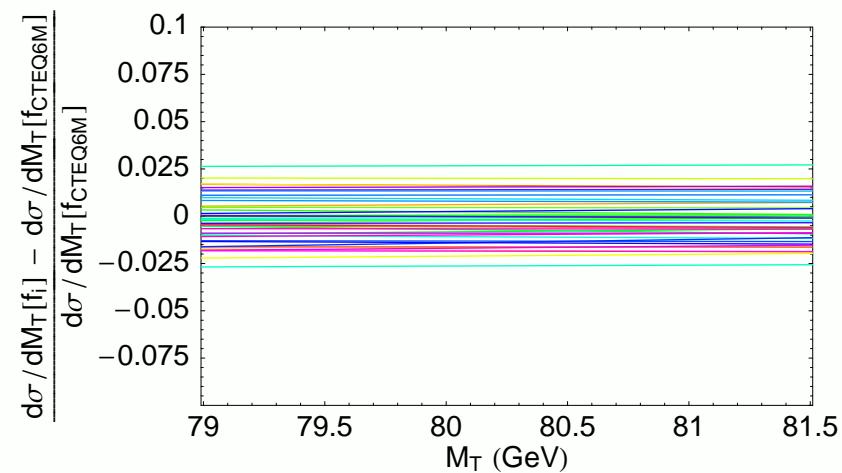
## PDF dependence of the ratio for $M_T$ distribution (VERY PRELIMINARY)

Combined  $W^+$  and  $W^-$  sample,  $-1 \leq y_e \leq 1$ ,  $p_{Te} > 25$  GeV

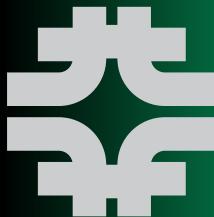
Raw ResBos output



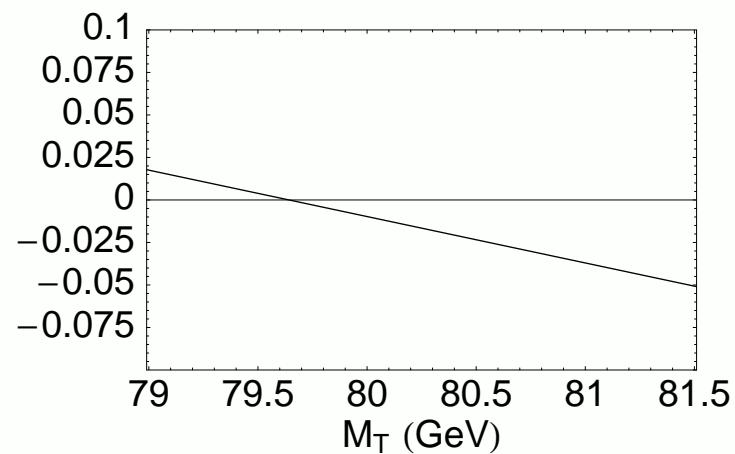
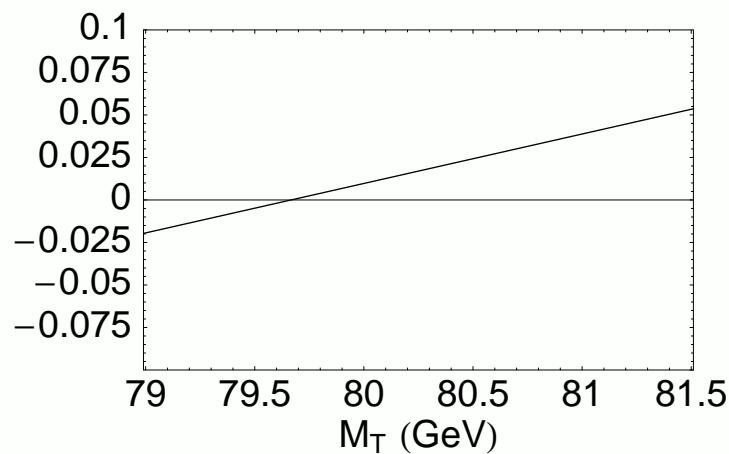
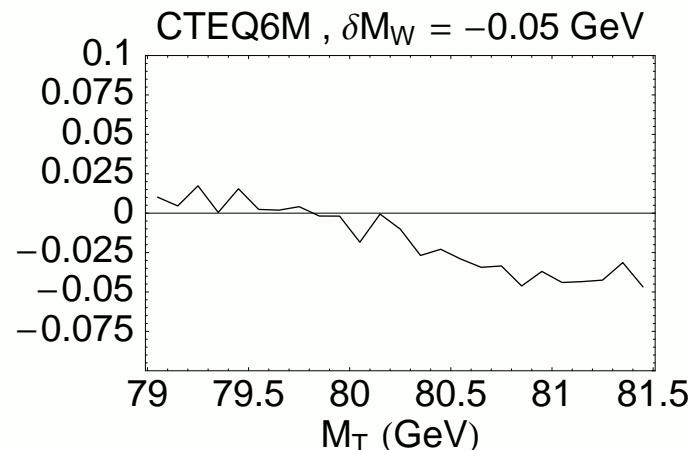
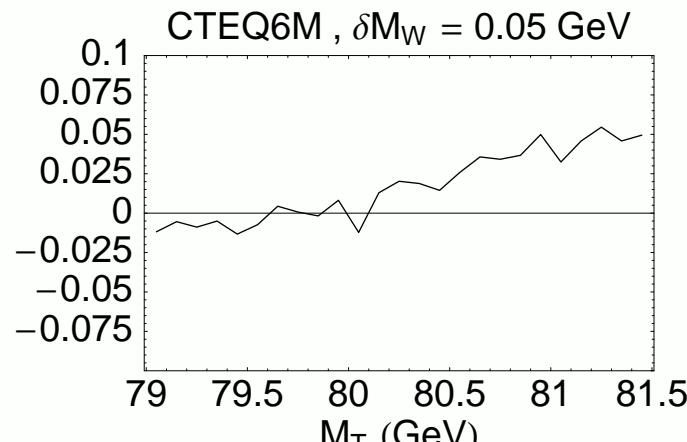
Linear fit



PDF variation changes normalization and not the slope



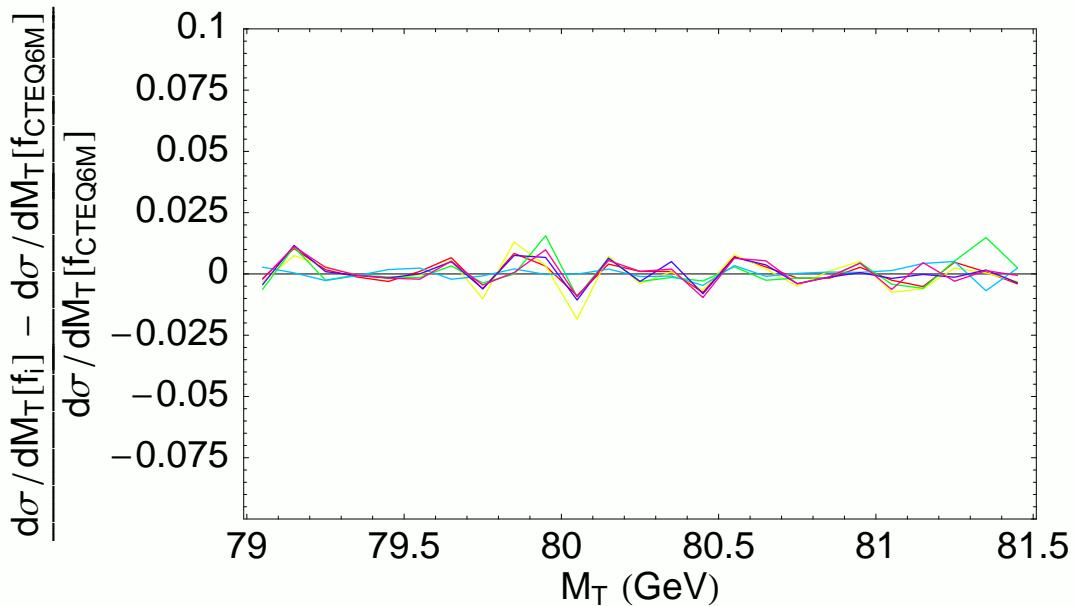
## Variation of $M_W$ by $\delta M_W = \pm 50$ MeV (VERY PRELIMINARY)



Visible variation in the slope (corresponding to the shift of the Jacobian peak)

$\therefore$  PDF error on  $M_W$  from  $M_T$  distribution is much smaller than 50 MeV

## Variation of $S^{NP}(b, Q)$ within the $1\sigma$ ellipse from the BLNY paper (VERY PRELIMINARY)



No visible change in slope

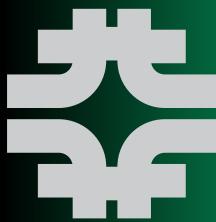
Note: The above error on  $S^{NP}(b, Q)$  (for  $\delta\chi^2 = 1$ ) underestimates the true error (dominated by systematic uncertainties)



Variations in the slopes of  $d\sigma/dM_T$  ratios  
**(VERY PRELIMINARY)**

| Source                | $\delta(\text{Slope})$<br>(pb/GeV $^2$ ) | Comparable<br>$\delta M_W$ (MeV) | Comments                         |
|-----------------------|--|----------------------------------|----------------------------------|
| $\delta M_W = 50$ MeV | 0.003                                    | 50                               |                                  |
| PDF error             | 0.002                                    | 5                                | $\delta\chi^2(\text{PDF}) = 100$ |
| $\delta S^{NP}(b, Q)$ | 0.0008                                   | 3                                | $\delta\chi^2(\text{BLNY}) = 4$  |

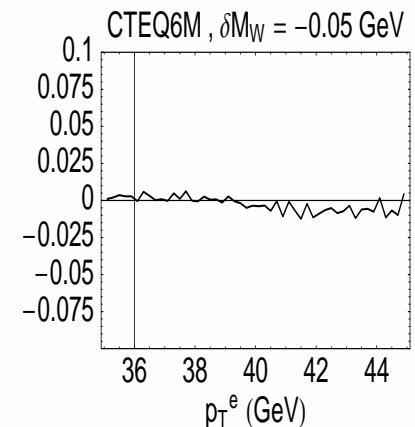
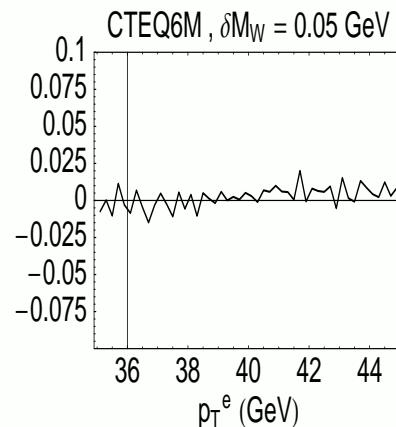
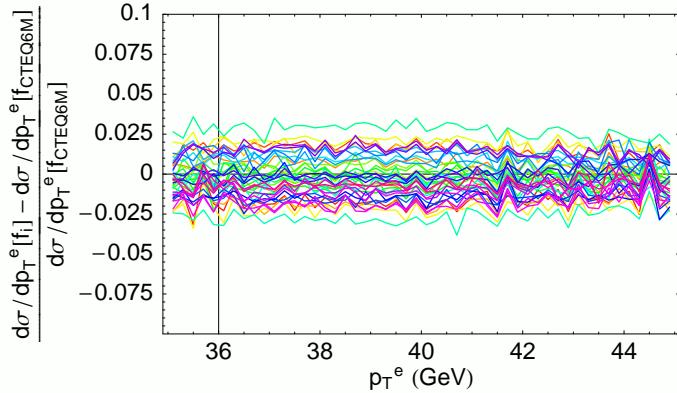
Monte-Carlo error is  $\sim 0.001$  (2 MeV)



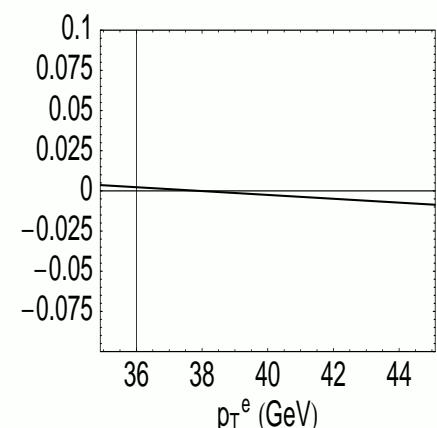
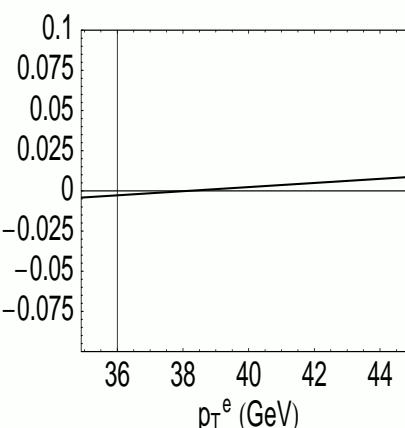
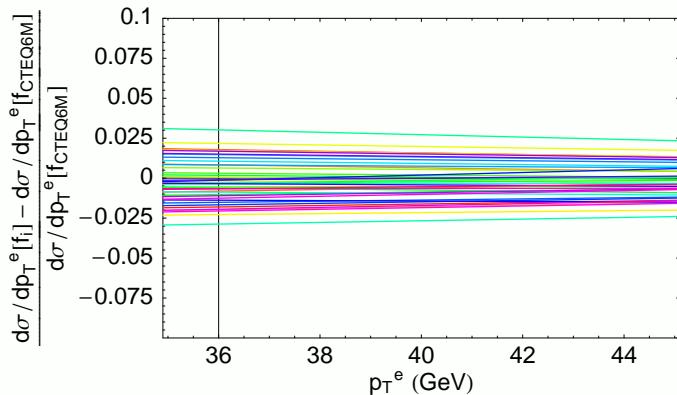
# PDF dependence of the ratio for the electron $p_T$ distribution (VERY PRELIMINARY)

Combined  $W^+$  and  $W^-$  sample,  $-1 \leq y_e \leq 1$ ,  $p_{Te} > 25$  GeV

## ResBos output



## Linear fit



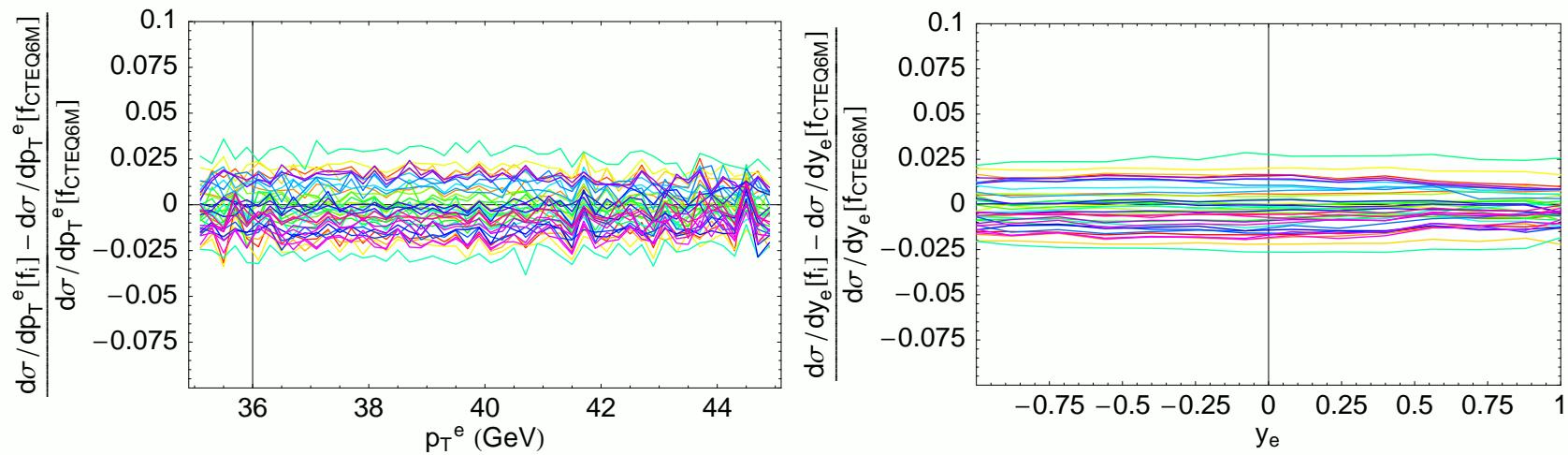


Variations in the slopes of  $d\sigma/dM_T$  ratios  
**(VERY PRELIMINARY)**

| Source                | $\delta(\text{Slope})$<br>(pb/GeV $^2$ ) | Comparable<br>$\delta M_W$ (MeV) | Comments                         |
|-----------------------|--|----------------------------------|----------------------------------|
| $\delta M_W = 50$ MeV | 0.0012                                   | 50                               |                                  |
| PDF error             | 0.0014                                   | 60                               | $\delta\chi^2(\text{PDF}) = 100$ |
| $\delta S^{NP}(b, Q)$ | 0.0008                                   | 30                               | $\delta\chi^2(\text{BLNY}) = 4$  |

Monte-Carlo error is  $\sim 0.00016$  (7 MeV)

## Correlation between $p_T^e$ and $y_e$ (VERY PRELIMINARY)



Better measurement of charge asymmetry will reduce the PDF error?